

# A New Design of Interpolator for Time to Digital Converter

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**Abstract** - We propose an alternative approach for time interpolation of (Time to Digital Converter)TDC in which a saw-tooth wave is generated instead of using sinusoidal wave in [10]. The proposed method avoids floating number operation for runtime as well as lowers the temperature variation caused by analog passive components. Since the differential portion of two projected signals is amplified, the wider range of time interval can be measured while preserving a few picoseconds resolution. Compared with the conventional analog interpolation, the proposed method using saw-tooth wave overcomes the drawbacks of conventional analog interpolation TDC by reducing the dependency on passive components which are sensitive to environment and operational conditions. It provides high repeatability and linearity property within a wide range of operation with high resolution of measurement. With the aid of proposed interpolation circuit, a practical TDC and its embedded measurement system are expected to be implemented. The experiment results demonstrate its feasibility and effectiveness for practical usage with a simple and low cost implementation.

**Index Terms** - Saw-tooth wave, Time to Digital Converter(TDC), Laser, Measurement, robust.

## I. INTRODUCTION

Time to digital converter(TDC) is a device which measures the infinitesimal time difference between rapid transit signals. Since the time of flight(TOF) of traveling light pulse is in proportion to distance to an object, TDC is required to be sensitive enough to measure picoseconds unit for target object in minimum distance.

Considering its cost and accessibility to passive components, the majority of TDC researches focus on analog interpolation rather than digital interpolation method.

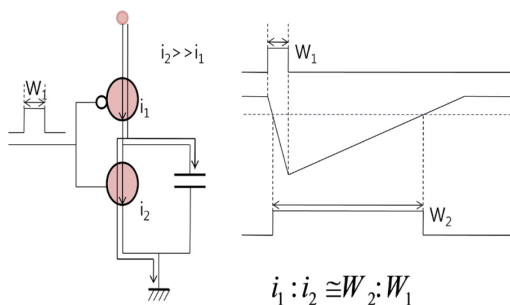


Fig. 1 Analog interpolation

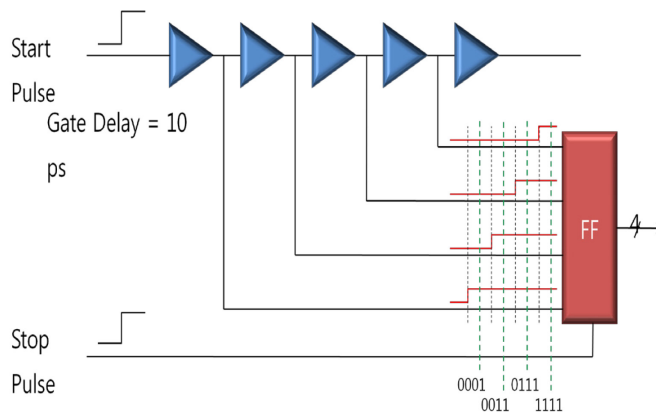


Fig. 2 Digital interpolation

As shown in Fig.1 analogue interpolation measures time by using low clock frequency after linearly expanding the minute time interval [2][4][5][6][11][12][13]. On the other hand, in Fig.2, digital interpolation method uses gate delay to estimate TOF for traveling light pulse [1][2][7][8][9][14][15][16].

While the measurement system using digital interpolation TDC ensures its precision and repeatability, its cost is mostly higher than the analog interpolation TDC equipment. Compare with digital interpolation, analog interpolation TDC is cost effective due to usage of cheap passive components. Despite of its cost effectiveness, however, the passive components used in analog interpolation TDC are sensitive to temperature variation causing measurement error. Moreover, the non-uniform parts of passive components induce additional error and difficulty in maintaining the expected repeatability of measurement. Instead of using passive components for analog interpolation, an oscillator can be used to generate sinusoidal waves for time interpolation, which avoids the above mentioned difficulties [10]. This method samples and holds sinusoidal wave at the time events of projection and receives triggering pulses. A drawback is that the sinusoidal wave is hard to catch its distortion and necessitates floating number operation.

We propose an alternative method for time interpolation of TDC in which a saw-tooth wave is generated instead of sinusoidal wave. The proposed approach avoids floating

number operation, as well as lowers the dependency on analog passive components to avoid temperature variation. Compare with capacitor voltage profile of Fig. 3 while charging and discharging, saw tooth wave provides wider linear interval for level capturing of signal, which in turn reduces distortion due to charge of environment.

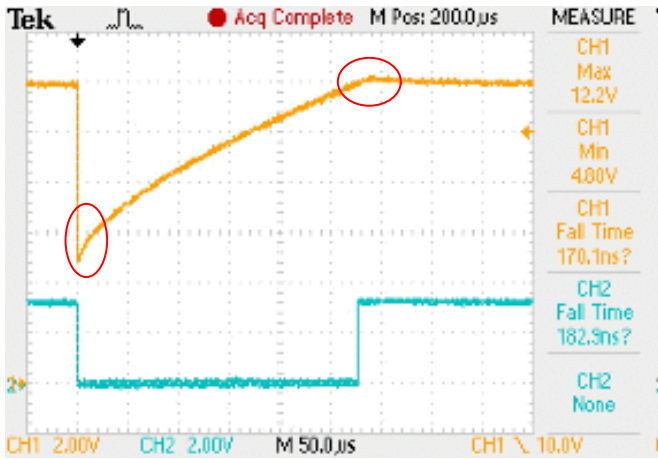


Fig. 3 Distortion of capacitor voltage profile

This implies that the use of saw tooth wave increases the reliability of measurement for industrial range sensors as LRF operating under hard environment conditions.

As shown in Fig. 4 and Fig. 5, since the differential portion of two projected signals is amplified, it has wider range of time interval and a few picoseconds resolution. It is also expected that the computational burden of DSP is decreased as well as its repeatability is enhanced.

## II. DESIGN OF SAW-TOOTH WAVE TDC

Fig.4 shows design concept of proposed TDC which measures TOF of traveling pulse using a saw-tooth wave.

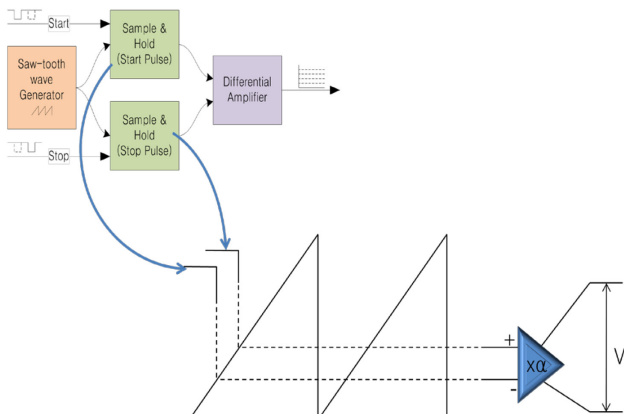


Fig. 4 Design concept of Saw-tooth Wave Based TDC

In Fig.4, the start signal triggers saw-tooth wave by sample/hold to input sampled level output to the negative input port of differential amplifier. Likewise, the stop pulse activates the operation of saw-tooth generator and sample/hold so that the projected saw-tooth voltage level can be submitted to the positive input port of differential amplifier. The

amplifier magnifies the small differential voltage signal of two inputs to the analog to digital converter. Assuming the saw-tooth wave with positive slope, the output of differential amplifier has positive value and it becomes larger as the time difference of traveling pulse increases. Fig.4 shows the design concept of interpolation in saw-tooth based TDC where the linear relation of input and output signals is identified before and after amplification.

## III. IMPLEMENTATION

Fig.5 shows an implementation of circuits which realizes the block diagram of TDC in Fig.4.

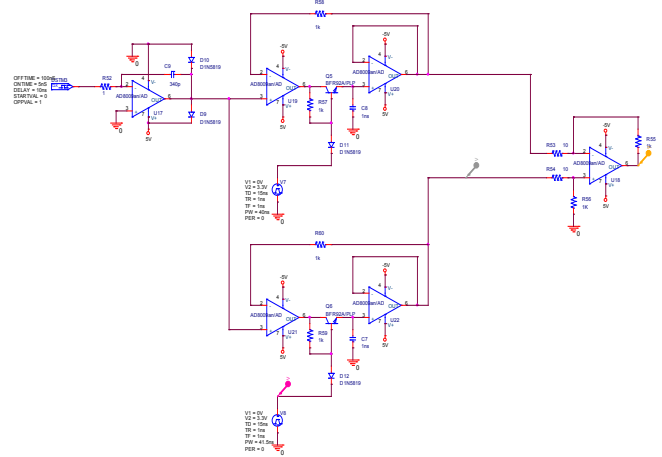


Fig. 5 An Implementation of TDC Blocks in Fig. 4.

In the figure designed are a saw-tooth generator, two sample and hold circuits, and a differential amplifier. The input signals to these circuits include a synchronizing clock for periodic generation of saw-tooth wave, start and stop pulses, and a reset input for initialization. The saw-tooth wave is sampled at the falling edges of start and stop pulses which are generated in an input synchronizing circuit. For the synchronizing circuit, flip-flops of FPGA are used as in Fig.6. In Fig.7, simulated synchronizing signals are shown for the flip-flop circuit.

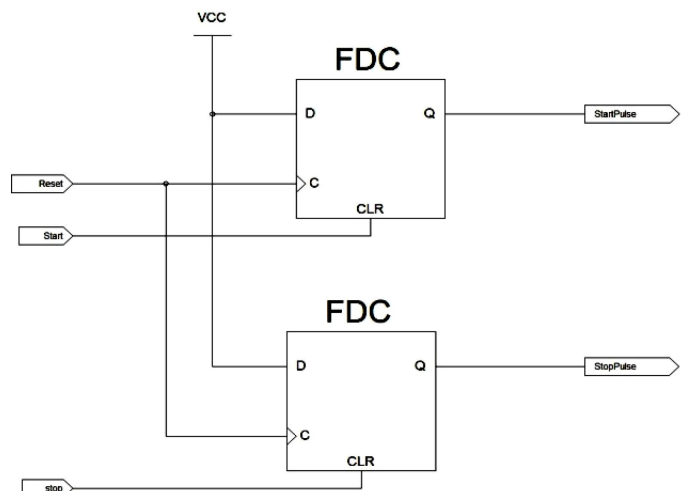


Fig. 6 Flip-flop Circuit for Synchronizing Signals

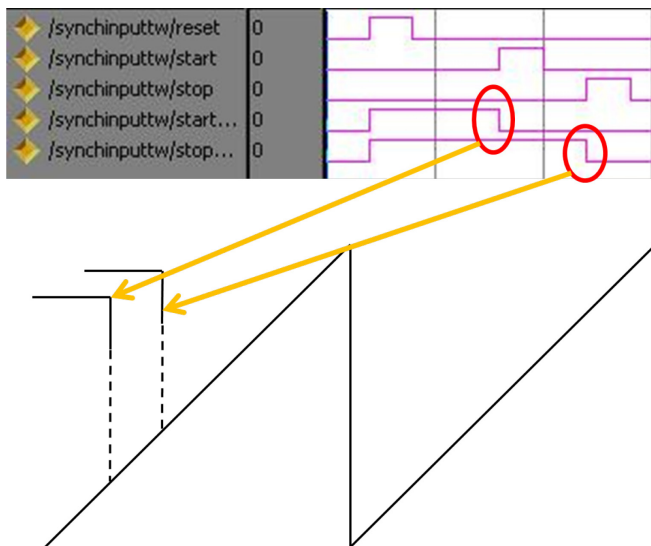


Fig. 7 Simulated Synchronizing Pulses.

Applying the synchronizing pulses to TDC circuit in Fig.5 the operation of measurement process was tested. After an input of start signal, three stop pulses with 500ps interval, shown in Fig. 8, are transmitted to the sample/hold circuit. In Fig.9, the linear relation of sampled saw-tooth voltage level is verified and their difference is amplified by differential amplifier.

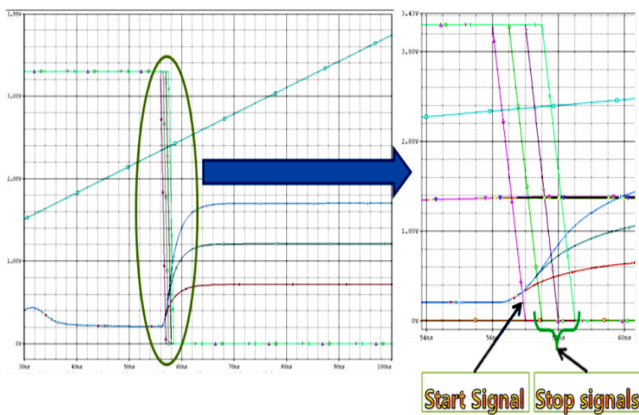


Fig. 8 Simulated input pulses

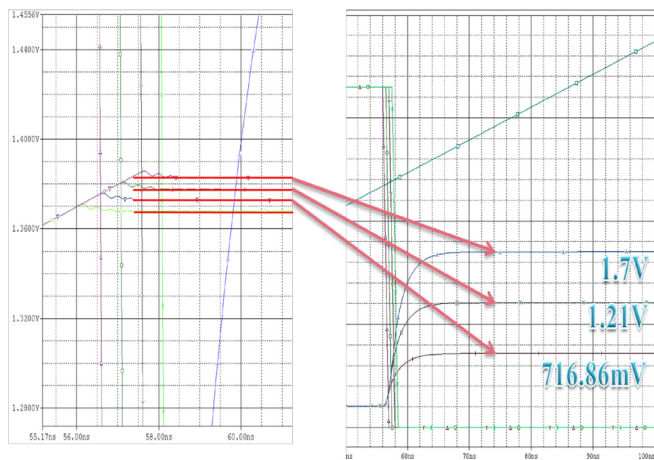


Fig. 9 Simulated Measurement Process

The differential voltage of sampled saw-tooth wave is 6mV for the time difference of 500ps between synchronizing start and stop signals. Similarly, the differential voltages of 10mV and 15mV correspond to 1ns and 1.5ns time differences, respectively. The outputs of differential amplifier for the three sampled signals are 716.86mV, 1.21V, and 1.7V, respectively, showing a constant increasing rate of about 500mV. In Fig.10, assuming the maximum voltage output of 5V, a 10bit ADC provides 4.88mV resolution per step corresponding to 4.88ps. When 12bit or 16bit ADC used, the resolution increases to 1.22ps or 0.076ps, respectively. Considering 1/2 LSB error of ADC, these resolutions amount to 9.76ps, 2.44ps, and 0.152ps, respectively, implying the measurement of distance less than mm unit is possible. The resolution of measurement can be also controlled by changing the amplification rate of differential amplifier. This method provides an alternative solution to high resolution measurement otherwise impossible with only a finite slope saw-tooth wave. In summary, our preliminary experiment verifies the effectiveness of using saw-tooth wave in fast and precision measurement of time interval for a wide range of traveling distance while maintaining fine resolution of measurement.

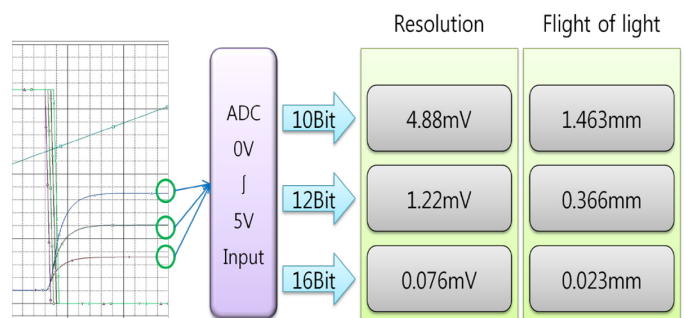


Fig. 10 Measurement Resolution

#### IV. CONCLUSION AND FURTHER WORKS

This paper presents design of a saw-tooth based interpolation circuit for TDC which overcomes the drawbacks of conventional analog interpolation method using passive components. The proposed interpolation reduces the dependency on passive components prone to be sensitive to environment and operational conditions. It provides high repeatability and linearity property within a wide range of operation and also supports high resolution of measurement. The experiment results demonstrate its feasibility and effectiveness for practical usage with a simple and low cost implementation.

Our further work is to design and implement a complete TDC and TDC embedded measurement system including ADC and digital logic circuits using FPGA and DSP.

#### ACKNOWLEDGMENT

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## REFERENCES

- [1] A. Mantyniemi, T. Rahkonen, and J. Kostamovaara, "A high resolution digital CMOS time-to-digital converter based on nested delay locked loops," *IEEE International Symposium on Circuits and Systems*, vol. 2, pp. 537-540, 1999.
- [2] E. Raisanen-Ruotsalainen, T. Rahkonen, and J. Kostamovaara, "An integrated time-to-digital converter with 30-ps single-shot precision," *IEEE International Symposium on Circuits and Systems*, vol. 1, pp. 278-281, 1999.
- [3] I. Nissinen and J. Kostamovaara, "Time-to-digital converter based on an on-chip voltage reference locked ring oscillator," *Instrumentation and Measurement Technology Conference*, pp. 250-254, 2006.
- [4] J. M. Rochelle and M. L. Simpson, "Current-mode time-to-amplitude converter for precision sub-nanosecond measurement," *Nuclear Science Symposium and Medical Imaging Conference*, vol. 1, pp. 468-470, 1992.
- [5] K. Maatta and J. Kostamovaara, "A high-precision time-to-digital converter for pulsed time-of-flight laser radar applications," *IEEE Transactions on Instrumentation and Measurement*, vol. 47, pp. 521-536, 1998.
- [6] Keunoh Park and Jaehong Park, "Time-to-digital converter of very high pulse stretching ratio for digital storage oscilloscopes," *Rev. Sci. Instrum.* 70, pp. 1568, 1999.
- [7] J. P. Jansson, A. Mantyniemi, and J. Kostamovaara, "A CMOS time-to-digital converter with better than 10ps single-shot precision," *IEEE Journal of Solid-State Circuits*, vol. 41, pp. 1286-1296, 2006.
- [8] K. Karadamoglou, N. P. Paschalidis, E. Sarris, N. Stamatopoulos, G. Kottaras, and V. Paschalidis, "An 11-bit high-resolution and adjustable-range CMOS time-to-digital converter for space science instruments," *IEEE Journal of Solid-State Circuits*, vol. 39, pp. 214-222, 2004.
- [9] M. D. Fries and J. J. Williams, "High-precision TDC in an FPGA using a 192-MHz quadrature clock," *Nuclear Science Symposium Conference*, vol. 1, pp. 580-584, 2002.
- [10] M. Lampton and R. Raffanti, "A high-speed wide dynamic range time-to-digital converter," *Review of Scientific Instruments*, vol. 65, pp. 3577-3584, 1994.
- [11] M. Tanaka, H. Ikeda, M. Ikeda, and S. Inaba, "Development of monolithic time-to-amplitude converter for high precision TOF measurement," *IEEE Transactions on Nuclear Science*, vol. 38, pp. 301-305, 1991.
- [12] M. Safi-Harb and G. W. Roberts, "Embedded measurement of GHz digital signals with time amplification in CMOS," *IEEE Transactions on Circuits and Systems*, vol. 55, pp. 1884-1896, 2008.
- [13] O. Sasaki, T. Taniguchi, T. K. Ohoka, and H. Kurashige, "A high resolution TDC in TKO BOX system," *IEEE Transactions on Nuclear Science*, vol. 35, pp. 342-347, 1988.
- [14] P. Palojarvi, K. Maatta, and J. Kostamovaara, "Pulsed time-of-flight laser radar module with millimeter-level accuracy using full custom receiver and TDC ASICs," *IEEE Transactions on Instrumentation and Measurement*, vol. 51, pp. 1102-1108, 2002.
- [15] Poki Chen, Shepz-luan Liu, and Jingshown Wu, "A low power high accuracy CMOS time-to-digital converter," *IEEE International Symposium on Circuits and Systems*, vol. 1, pp. 281-284, 1997.
- [16] S. Tisa, A. Lotito, A. Giudice, and F. Zappa, "Monolithic time-to-digital converter with 20ps resolution," *Solid-State Circuits Conference*, pp. 465-468, 2003.